

Objectives

- Understand that recognising a problem is the first step in solving it
- Categorise different types of problem and solutions
- Explore different strategies for problem-solving
- Understand the concept and application of the "divide and conquer" approach

Recognising the problem

- Before a problem can be solved, it has to be recognised
- That's how all great inventions are made!
- What problems does this picture make you think of?
- Have they been solved?



I forgot my password!

- When you buy something online from a site on which you have previously registered, you will almost certainly be asked for your password
- More than one-third of customers admit to pulling out of a transaction because they can't remember their password
 - MasterCard recognised that this is a problem that needs to be solved
 - What solutions can you suggest to solve this problem?



The MasterCard solution

- When you try to purchase something, a push notification prompts you to look into your camera and blink
- That's it you're done
 - Why do you need to blink?
 - Is this a good solution to the problem?



Types of problems

- Some problems rely heavily on mathematics for a solution
 - Keeping a message secure by encrypting it is one problem that has been solved in many different ways
 - One method relies on having a key which is the product of a very large prime number
 - It takes a huge amount of computation time to find the numbers
- What other methods of encryption do you know about?
 - Can any encrypted message be decrypted, given enough time?

Pattern recognition

- Pattern recognition is a computational problem used in hundreds of different applications
 - Medical diagnosis
 - Speed cameras
 - Detecting a dangerously overcrowded platform on an Underground railway
- Can you think of some other uses for pattern recognition?
- Are all problems computable?



Non-computable problems

- Problems such as face-recognition or flying an airliner across the Atlantic with no human intervention may once have seemed noncomputable, but are now routinely solved
- However, Alan Turing proved in 1936 that some problems are non-computable
 - Computer Science is sometimes defined as "the study of problems that are and are not computable"



Sample problem

 You are given nine sweets and four paper bags

 You are required to place an odd number of sweets in each bag

 Can you come up with a solution?

> Note: All sweets are to be used and none eaten!



The solution

- It's impossible!
- Can you explain why?
- If you had 2,675 sweets and 1000 paper bags, would it be possible to find a solution?
- Write down a solution if you had 99 sweets and 29 paper bags

Worksheet 5

Try Task 1 on the worksheet

Methods of problem solving a problem,

including:

trial and error

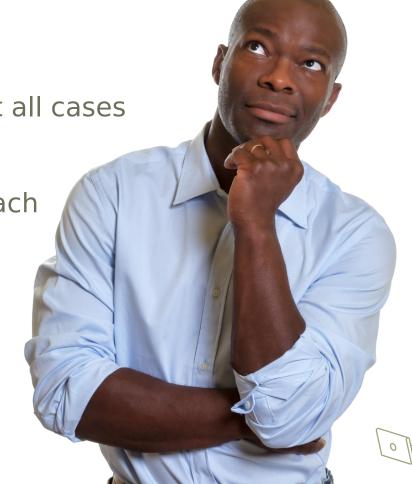
enumeration – list all cases

simulation

theoretical approach

creative solution

and many more



Simulation problems

- Simulation is the process of designing a model of a real system in order to understand the behaviour of the system, and to evaluate various strategies for its operation
- Simulation applications include:
 - Financial risk analysis
 - Amusement park rides
 - Population predictions
 - Managing inventory systems
 - Queueing problems



Enumeration example

Finding solutions to anagrams

Enter a word into an 'anagram solver' website and it will tell you all the possible anagrams of the word
How does it do this?



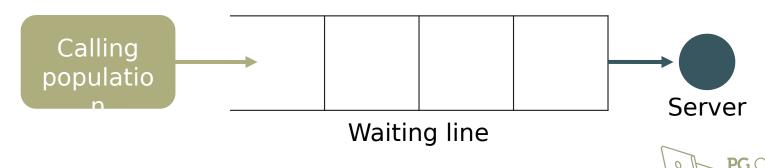
Queueing problems

- How would you find the optimum number of
 - Call centre help lines?
 - Checkouts at a new supermarket?
 - Paypoints on a toll road?
 - What other queueing problems might need to be solved?



Simulation of queueing systems is described by

- The arrival rate
- Time between arrivals
- Number of servers
- Service time
- Arrival rate must be less than service rate for a stable system



Alternative approaches

 Suppose you were a motorbike rider planning a stunt jump over a ravine

 You know the height of the jump ramp

 You know the length of the run up to the range

 How can you be sure to clear the gap?

 Would you favour a trial and error approach, or a theoretical approach?



Creative solution

 How would you prevent any comments from Internet Trolls from reaching their intended recipients if you ran Twitter?

> What would constitute a comment deemed to be from a troll and worthy of concealing from the recipient?

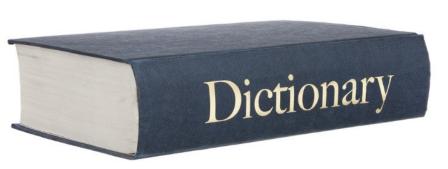


Worksheet 5

Try Task 2 on the worksheet

Strategies for algorithm design conquer' is a very efficient

- strategy
- This involves finding a solution to a sequence of smaller, related problems until the instance is small enough to be solved directly
- Suppose you want to look up the meaning of "meander" in a hard-copy dictionary
 - What w



ight page?



Divide and conquer

- Open the dictionary somewhere near the middle
- If "meander" is on that page, you have found the right page
- If you are on a page with words beginning n-z, you can discard that half of the dictionary and open a page between a-m
- Continue discarding approximately half the remaining pages until you find the correct one



Binary search

- This is the principle of the binary search
- The middle name is examined first, and if that is not the name sought, half the list is discarded
 - Which items would need to be examined to find the name Zane in this list of names?

Arthur Chloe Daisy Eric Holly Jon Liam Mark Rowan Zane



Try it out!

- Ask a partner to think of a number between 1 and 100
- For each guess you make, your partner will tell you whether you are too high, too low or on the button
 - How many guesses will you need?
 - How many if the number is between 1 and 1024?
 - How many guesses, on average, using a sequential search?



Sample problem

A well-known celebrity is among a group of people at a gathering. The celebrity knows none of the other guests, but everybody knows the celebrity

 How can you identify the celebrity by repeatedly asking the question "Do you know this person?"

The other guests may, or may not know each other



Solution

- If there are n (where n = 2 or more) people at the gathering, you can select two people from the group, and ask one of them (Person A) "Do you know this person?" (Person B)
- If A knows B, then remove A from the people who could be the celebrity. If A does not know B, remove B from the group who could be the celebrity.
- Then solve the problem for the remaining group of n-1 people
- Repeat until there are only 2 people left

Worksheet 1

Now try Tasks 3 and 4 on the worksheet

Plenary

- There is an infinite number of different realworld problems to be solved, from making this week's shopping list to deciding on the nation's best economic strategy for the next decade
- Computational thinking is a way of thinking about how to approach problems and finding optimum solutions
- Abstraction is used in problem solving to remove unnecessary details from the problem and in procedural decomposition, identifying sub-procedures necessary to solve the

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